

# Performance Analysis of FPGA based Implementation of FFT Architecture with Pruning Algorithm for Industrial Applications

P.Suresh Kumar<sup>1</sup>, S.Meenakshi<sup>2</sup>

<sup>1</sup>Department of Electrical and Computer Engineering,, Mahendra Engineering College (Autonomous)  
Mahendhirapuri, Mallasamudram - 637 503, Namakkal District, Tamil Nadu, India

<sup>2</sup>Department of Electrical and Computer Engineering, Mahendra College of Engineering,  
Salem, Tamilnadu, India

**ABSTRACT:** In the present study the improved architecture of Inverse Fast Fourier Transform (FFT) is developed and presented. The number of arithmetic operation is more in the normal working of conventional Inverse Fast Fourier Transform. An enhanced pruning algorithm is utilized to reduce the number of arithmetic operations in the FFT architecture. The performance of the improved FFT architecture is estimated to find its suitability for the low power Wireless communication system. It was implemented in 8-point FFT architecture using decimation in frequency algorithm using hardware description language. It is implemented in XC7z020clg484-1 from Zynq-7000 family with a frequency of 220MHz. It is found that the improved FFT architecture reduces maximum of 40% of the arithmetic operations, which reduces the power consumption by maximum of 10%. Hence, the improved FFT architecture could be used in the signal processing units in wireless applications.

**KEYWORDS:** Inverse Fast Fourier Transform (FFT), Orthogonal frequency division multiplexing (OFDM), Enhanced Pruned Algorithm (EPA), Field-programmable gate array (FPGA), Quadrature amplitude modulation (QAM).

<https://doi.org/10.29294/IJASE.7.2.2020.1770-1775>

© 2020 Mahendrapublications.com, All rights reserved

## 1. INTRODUCTION

The developments in the area of wireless communication technology are introducing more challenges and opportunities for the researchers in the recent days. The continuous growth of internet traffic which demands for high transmission rates motivates for the design of various wireless networks. Offset Quadrature Amplitude Modulation (OQAM) transmitter is found to play a dominant role in the wireless communication system to meet the challenges of the future systems. This paper aims to reduce the power and complexity of Inverse Fast Fourier Transform block at wireless communication system. The advancements in VLSI design and signal processing enhances the energy efficiency and reduction in the design complexity in the transmitter. Razavi et. al.[1] reported the capacity of OFDM/OQAM evaluated by isotropic orthogonal transfer method through information theoretic analysis. The spectral efficiency of developed OFDM/OQAM and conventional OFDM were evaluated. Complexity of the system has to be decreased. Chuanxue et al [2] presented architecture of conjugated transmission system for FBMC/OQAM. The frequency and time prototype filter for Offset

Quadrature Amplitude Modulation with better spectral shape and mobility support was reported by Jeremy Nadal et.al [3]. This paper presents a better performance of FBMC/OQAM for obtaining linear combination diversity.

Moreover, Guillem et al [4] and Jeong-Min Choe et.al [5] explained the comparison of modulation schemes used for the modern wireless communication system. The Channel estimation and improved spectral efficiency is also presented. Trung-Hien Nguyen et al [6] presented the frequency sampling equalizer used for the chromatic dispersion compensation where an adaptive maximum likelihood estimator was utilized for the phase noise compensation. The trade-off analysis was also made between chromatic dispersion and phase noise compensation. Amir Aminjavaheri et al [7] studied an asymptotic study of the performance of filter bank multicarrier in the context of massive multi-input multi-output. An efficient equalization method presented for the arbitrarily large signal to interference plus noise ratio values by increasing the number of base stations (BS) antennas. The design of multiple input multiple output de-coding and pre-

\*Corresponding Author: sureshk.eee@gmail.com

Received: 10.10.2020

Accepted: 28.10.2020

Published on: 01.11.2020

Suresh Kumar & Meenakshi

coding matrices for Filter Bank Multicarrier System was reported by Marius Caus and Perez-Neira[8]. The bit error rate was improved than the existing MIMO-FBMC/OQAM Scheme. The decomposition design of complex training sequence for an efficient estimation of channel in Multiple-Input Multiple-Output multicarrier communications using OQAM was reported by Su Hu et al [9]. The Simulation results were validated by Uma Maheswari et.al.[10] presented the analysis of multicarrier communication system with non-linear power amplifiers for modern wireless communication system.

Rodolfo Gomes et.al [11] reported the performance analysis of FS-FBMC versus OFDM for better data rate applications. An orthogonal frequency division multiplexing (OFDM) model was designed to standardize for an IEEE standard data-rate applications. Martin and Peissing [12] studied the capacity gains for Single and Multiuser channel adaptive waveforms in FBMC/OQAM systems. The cell and user-specific channel adaptive waveforms provided a low-complexity system design, which was capable of fighting the interference problem for systems without a cyclic prefix. Jeremy et al [13] explained a complexity reduced architecture for FBMC/OQAM Transmitter. A transmitter with pipelined design is able to support different type of filter length aims less complexity in design.

Hyungju Nam et.al [14] reported a multicarrier system for QAM transmission and reception with two prototype filters. The bit error rate and signal-to-interference power ratio were evaluated for FBMC/QAM. Ji-Hyun Moon et.al [15] explained Peak-to-Average-Power-Ratio reduction in the FBMC-OQAM System. Reduction of power in FBMC/OQAM was numerically evaluated using simulations. Han Wang et.al [16] presented Hybrid Peak to Average Power Reduction Scheme for FBMC/OQAM. Multi data scheme provided 0.2dB peak to average power reduction performance than hybrid power transmit sequence transmit sequence in the simulation results. The VLSI architecture for fast Fourier transforms (FFT) processor capable of generating normal output order sequence reported by Yun-Nan Chang [17]. The normal output order sequence was generated by a sequence conversion method. The power efficient hardware was generated with less number of adders. Power and complexity need to be decreased. Madheswaran et.al [18] reported the power efficient modified FFT for wireless transmitter. The architecture was designed and verified using the hardware description language. Nguyena et al, Hu et al [19,20] explained the designs for the FFTs and FFTs with high speed, better complexity and improved utilization of resources for wireless communication transmitters.

Zhong Hu and Honghui Wan explained how to save power consumption and complexity in computation by a traced FFT pruning [20]. This input pruning TFFTP to biological sequence is aligned. Moreover, a study of an FFT core for various wireless modems designed and implemented. The optimization and conversion of C code to hardware is analyzed. The resulting hardware is optimized to IP core available in Xilinx FPGA in terms of hardware requirements. This present work explains the default implementation by Vivado TM HLS which minimizes the resource consumption. It gives high latency and minimal parallelism which generates good results, but need more improvement in power consumption.

It has been reported an OFDM transceiver chip is designed by HDL. This work used with wireless communication system for high speed operations. The high band width capabilities of OFDM have an advantage on wireless products with many types of networking systems. Moreover, the modulator for the Filter Bank Multi Carrier system showed less complexity than the traditional one. FFTs implemented for the FBMC modulator is a pruned circuit. It gives the advantages to the complex conjugation relations formulating the outputs for the FFT stage. Relations depend on the delay parameters. When it is even values, FFT will take the real value as the input. For odd values, there is complex conjugation relation between even and odd indices of the FFT output. Complexity is higher in this presented method. Multiplications in FFT are replaced by pass logic in wireless applications is presented recently. It reduces power by 6.5% for 64 point FFT and is implemented in VLSI. Minimum bit resolution map of FFT/FFT architectures are reported. The high accuracy and validity of identified bit resolution map is experimentally verified in FPGA based platforms.

### 1. Enhanced Pruned Algorithm (EPA) for FFT

FBMC/OQAM transmitter diagram is shown in Fig.1. This method of transmission is able to achieve full time/ frequency efficiency through the use of Offset Quadrature Amplitude Modulation. Maximum QAM samples are modulated based on the number of active sub-carriers and unused carriers are set to zero. PPN is poly phase network. Polyphase network re-generates the odd samples from the computed even samples.

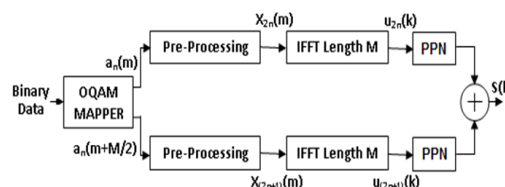


Fig.1 Block diagram of OQAM

To reduce the operational complexity, the output indices of the enhanced pruned algorithm with FFT are applied together with a decimation-in time (DIT) algorithm. The basic computation part of FFT was done by butterfly method. These arithmetic operators are used for complex computation and twiddle factor calculation. A general N point FFT computes  $O(N \log N)$  number of operations.

The conventional FFT algorithms were not an efficient method for unwanted operations on zero input values. In general, the system demands operation with high speed and low power consumption for all combination of inputs. Efficiency of the Inverse Fast Fourier Transform technique can be increased by designing the conventional FFT with enhanced pruning algorithm which is proposed in this paper. The speed of the FFT is increased by removing few operations of output whose input and output values are zero. Those operations are deprecated for the corresponding inputs in the process of pruning. These pruning techniques were added to filter bank system in OQAM transmitter for reducing the operating power and complexity of the system.

The N-point Inverse Fast Fourier Transform with  $0 \leq n \leq N-1$  is given by

$$x(n) = \frac{1}{N} \sum_{k=0}^{N-1} X(k) e^{j2\pi kn/N}$$

$$= \frac{1}{N} \sum_{m=0}^{N/2-1} X(k) W_N^{-kn}$$

The kernel  $W_N^{-kn}$  with

$$\{k, n \in \mathbb{Z} \mid 0 \leq k, n \leq N-1\}$$

$$W_N^{-kn} = e^{-j(2\pi/N)kn}$$

The equation (2) can be decomposed into two sums:

$$x(n) = \frac{1}{N} \sum_{m=0}^{N/2-1} X(2m) W_N^{-2mn} + \frac{1}{N} \sum_{m=0}^{N/2-1} X(2m+1) W_N^{-n(2m+1)}$$

Butterfly unit with radix 2 FFT is shown in Fig.2

A and B are the inputs and X and Y are outputs of 2-radix FFT algorithm. The twiddle factor is  $W_N$ .

The outputs are,

$$X = A + BW_N \quad (5)$$

$$Y = B - BW_N \quad (6)$$

Tariq Jamil [21] reported the conversion of complex numbers to binary number system for the operation and combining of real and imaginary numbers to complex numbers for various operations.

Equation for the total power consumption in terms of dynamic component and static component is given in the equation (7).

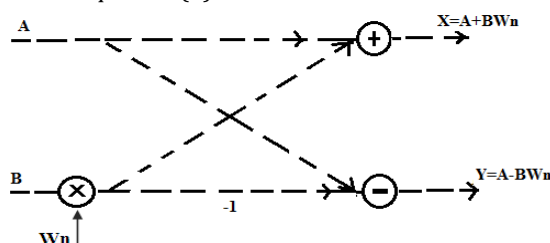


Fig.2 Butterfly diagram of radix-2 FFT

$$P_{total} = P_{dynamic} + P_{static} = ar f_c C_L V_{DD}^2 + I_{off} V_{DD}$$

$C_L$  load capacitance,  $V_{DD}$  supply voltage,  $I_{off}$  leakage current,  $f_c$  is the clock frequency and  $ar$  is the switching probability called activity ratio. Dynamic power dissipation occurs only when the circuit is in the working mode. i.e. the circuit is executing some task on a set of data. In this paper, an enhanced pruning method is proposed to reduce the dynamic power by reducing the number of switching operations.

Number of adders used in each stage of computation is 4. Number of subtractors and multipliers also used in the each stage is 4. Total number of adders, subtractors and multipliers in total stages of operation is 12. Maximum number of computations can be performed by one adder is 4. Number of computations can be performed by the four adders in the first stage of computation is 16. Number of operations can be performed by the subtractor and multiplier in each stage is also 16. Maximum number of addition operation in the whole 8 point FFT system is 48. In partial pruning algorithm, whenever the inputs and outputs go to zero, operations for the respective inputs were omitted [20]. The total number of complex multiplication and additions are reduced by this partial pruning method. In partial pruning method, number of addition operations is reduced to 12 from actual 16. Likewise number of multiplications and subtractions are also reduced to 12 in each stage. The total number

of operations in 8 point FFT is reduced to 108 from 144. Maximum 36 number of operation are avoided based on the partial pruning method. By omitting the number of operations, power consumption also reduced.

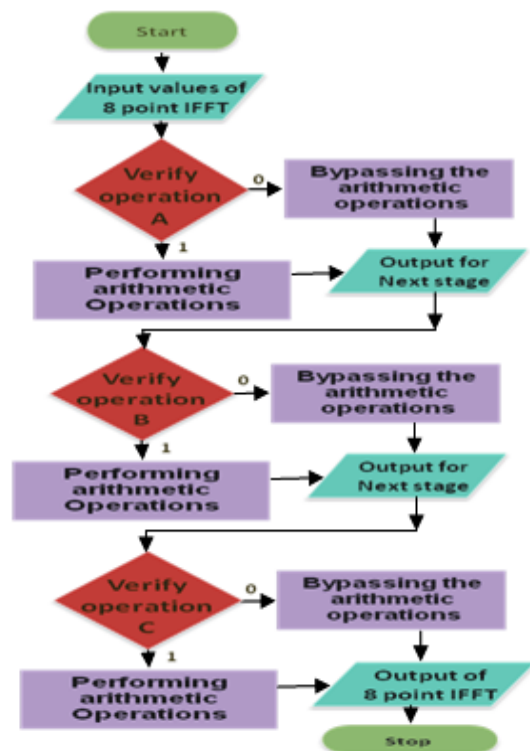


Fig. 3 Flow Chart of Enhanced Pruned Algorithm for Subtractor operator in FFT

## 2. RESULTS & DISCUSSION

Number of operations in addition, subtraction and multiplication is explained in three stages of operation using butterfly diagram. 16 numbers of operations were performed for addition, subtraction and multiplication in conventional FFT in the first stage. Likewise total of 48 operations are performed in each stage of FFT. Total of 144 numbers of operations are performed in the conventional FFT. In partial pruning operation 48 numbers of operations in each stage is reduced to 36. So, total operations in three stages are reduced to 108. 40 numbers of operations are reduced in partial pruning FFT operation than conventional FFT. Number of operations in the Enhanced pruned FFT is reduced to 32 from 48 during the first stage of operation than conventional FFT. Number of operations are reduced to 32 in the remaining stages of Enhanced pruned FFT. Total number of operation in the enhanced FFT is reduced to 96. It is the minimum number of operations in the FFT with enhanced pruned

algorithm. Comparison between the different number of operations of proposed technique with conventional and partial pruned FFT in different order FFT is given in Table 1. Total of 144 operations are performed in 8 point FFT.

Table 1 Comparison of number of operations in various 8-point FFT

Stages of FFT	Operations	Conventional FFT	Partial Pruned FFT	Enhanced Pruned FFT
Stage 1	Additions	16	12	12
	Subtractions	16	12	8
	Multiplications	16	12	12
Stage 2	Additions	16	12	12
	Subtractions	16	12	8
	Multiplications	16	12	12
Stage 3	Additions	16	12	12
	Subtractions	16	12	8
	Multiplications	16	12	12

Number of operation in the partial pruned FFT in 16 point FFT is 288. An operation in the proposed technique is reduced to 248. 136 operations are reduced in the proposed technique than conventional FFT in 16 point FFT. Maximum of 40% operations are reduced in the proposed technique than conventional FFT in all order of FFT. Power consumption for the proposed algorithm with the FFT is 78mW.

The architecture of the Enhanced pruned FFTs are designed in hardware description language and synthesized in the XC7z020clg484-1 from Zynq-7000 family. Synthesis results are given in Table 6. These results are based on the FFT size of 512. The complexity of the proposed design is relatively inconsiderable when the proposed FFT size is increased. Overall power reduction is done by proposed FFT with conventional FFT.

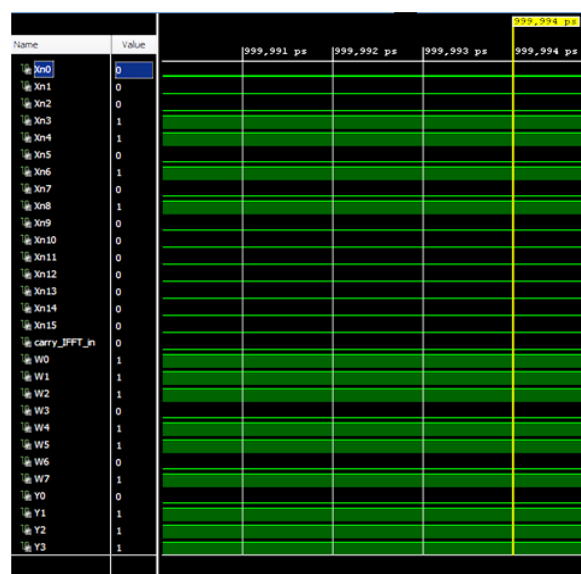


The transmitters are implemented on the Zed-Board using the method given in [11]. Power consumption generated for the proposed technique is given in the table-6. Power consumed for the conventional FFT was 88mW [13]. Proposed logic generates very less complexity with utilization compared to the last technique which was developed for the FFT in FBMC/OQAM transmitter.

**Table 2 Comparison of Power Consumption**

Transmitter Architecture	Power (mW)
Conventional FFT [13]	88
FFT using Enhanced Pruned Algorithm (Proposed)	78

Output wave form for the proposed algorithm with 8 point FFT is given in the Fig.4, which is generated by the XC7z020clg484-1 device for the proposed algorithm. The proposed algorithm is implemented using hardware description language. So, these wave form values are generated after less number of addition, subtraction and multiplication operations in the device. Overall power consumption will be reduced in the FBMC/OQAM transmitter by this FFT with the enhanced pruned algorithm. Speed of the system is also increased by reducing the propagation delay between the blocks by bypassing or omitting the number of operators by the enhanced pruned algorithm used in the FFT design.



**Fig.4. Output Waveform of 8-point FFT using Enhanced pruned algorithm**

### 3. CONCLUSION

In this work, an enhanced pruned algorithm for the FPGA implementation of Inverse Fast Fourier Transform is proposed. These enhanced pruned FFTs reduce the complexity in the architecture. Number of arithmetical operators in FFTs was reduced by maximum of 40% using this enhanced pruned algorithm. For comparison purpose, conventional FFT and some pruned FFTs have been considered from the previous work. Analytical studies of FFTs using these algorithms were demonstrated with reduction in complexity and power consumption. Analytical and implementation results for the proposed architecture have demonstrated the reduction in complexity and power consumption which are compared. Behavioral level of design leads to minimize the complexity and increases the speed of operation. Power consumption of proposed algorithm is reduced by a maximum of 10% of the conventional FFT design. These algorithms were implemented using VHDL in XC7z020clg484-1 from Zynq-7000 family with a clock frequency of 220MHz. Power reports and utilization statements are generated by implementing in the targeting device XC7z020clg484-1 from Zynq-7000 family.

### REFERENCES

- [1] Razavi, M R., Xiao, P., Tafazolli, R. 2015. Information theoretic analysis of OFDM/OQAM with utilized intrinsic interference, IEEE Signal Process. Lett., 22(5) 618-622.
- [2] Chuanxue Jin; Su Hu ; Yixuan Huang; Fan Li; Jing Zhang; Shiyong Ma. 2017. On design of conjugated transmission scheme for FBMC/OQAM systems with interference cancellation, China Communications, 14(8) .
- [3] Jeremy Nadal, Charbel Abdel Nour, Amer Baghdadi, 2018. Design and Evaluation of a Novel Short Prototype Filter for FBMC/OQAM Modulation, IEEE Access, 6, 19610-19625.
- [4] Guillem Femenias, Felip Riera-Palou, Xavier Mestre, Uan J. Olmos Downlink Scheduling and Resource Allocation for 5G MIMO-Multicarrier: OFDM vs FBMC/OQAM, IEEE Access, 5, 13770-13786, 2018.
- [5] Jeong-Min Choi; Youngho Oh; Hakju Lee; Jong-Soo Seo Pilot-Aided Channel Estimation Utilizing Intrinsic Interference for FBMC/OQAM Systems, IEEE Transactions on Broadcasting, 63(4) 644-655, 2017.
- [6] Trung-Hien Nguyen., François Rottenberg ; Simon-Pierre Gorza Efficient Chromatic Dispersion Compensation and Carrier Phase Tracking for Optical Fiber FBMC/OQAM Systems, IEEE Journal of Lightwave Technology, 35(14) 2909-2916, 2018.

- [7] Amir Aminjavaheri, Arman Farhang, Behrouz Farhang-Boroujeny. 2018. Filter Bank Multicarrier in Massive MIMO: Analysis and Channel Equalization, IEEE Transactions on Signal Processing, 66(15) 3987-4000.
- [8] Marius Caus, Perez-Neira, 2014. Multi-Stream Transmission for Highly Frequency Selective Channels in MIMO-FBMC/OQAM Systems, IEEE Transactions on Signal Processing, 62(4) 786 - 796, February.
- [9] Su Hu, Zilong Liu, Yong Liang Guan, Chuanxue Jin, Yixuan Huang, And Jen-Ming Wu, 2017. Training Sequence Design for Efficient Channel Estimation in MIMO-FBMC System", IEEE Access, 5, 4747- 4758, April.
- [10] Govindaraju Uma Maheswri, Ananthi Govindasamy, Sundarrajan Jayaraman Thiruvengadam, 2017. Performance analysis of filter bank multicarrier system with non-linear high power amplifiers for 5G wireless networks, IET signal processing, 11(1) 66-72, February.
- [11] Rodolfo Gomes, Joao Reis, Zaid Al-Daher, Akram Hammoudeh, Rajael F.S. Caldeirinha, 2018. 5G: performance and evaluation of FS-FBMC against OFDM for high data rate applications at 60 GHz, IET signal processing, 12(5) 620-628, June.
- [12] Martin Fuhrwerk, Jurgen Peissing, 2018. Capacity Gains for Single- and Multi-User CAW in FBMC-OQAM Systems, IEEE Communications Letters, 22(1) January.
- [13] Jeremy Nadal, Charbel Abdel Nour, Amer Baghdadi Low-Complexity Pipelined Architecture for FBMC/OQAM Transmitter, IEEE Trans. Circuits and Systems, 63(1) 2016.
- [14] Hyungju Nam, Moonchang Choi, Seongbae Han, Chanhong Kim, Sooyong Choi, Daesik Hong, 2016. A New Filter-Bank Multicarrier System with Two Prototype Filters for QAM Symbols Transmission and Reception, IEEE Transactions on wireless communications, 15(9) 5998-6009, June.
- [15] Ji-Hyun Moon, Ye-Ri Nam, Jeong-Ho Kim, 2018. PAPR Reduction in the FBMC-OQAM System via Segment-based Optimization, IEEE Access, 6, 4994-5002, January.
- [16] Han Wang; Xianpeng Wang; Lingwei Xu; Wencai Du, 2016. Hybrid PAPR Reduction Scheme for FBMC/OQAM Systems Based on Multi Data Block PTS and TR Methods, IEEE Access, 4, 4761-4768, September.
- [17] Chang, Y.-N. An efficient VLSI architecture for normal I/O order pipeline FFT design, IEEE Trans. Circuits Syst. II, Exp. Briefs, 55(12) 1234–1238, 2008.
- [18] Madheswaran, M., Abraham C G, Manoj Sharma, Power Reduction in OQAM transmitter architecture using modified FFT, Proc. of the IEEE International Conference on Emerging devices and smart systems (ICEDSS), India, March, pp. 1-5, 2017.
- [19] Ngoc Hung Nguyen, Sheraz, Ali Khan, Cheol-Hong Kim, Jong-Myon Kim, 2018. A high-performance, resource-efficient, reconfigurable parallel-pipelined FFT processor for FPGA platforms, Microprocessors and Microsystems, April 2019.
- [20] Hu, Z.; Wan, H. 2005. A Novel Generic Fast Fourier Transform Pruning Technique and Complexity Analysis, IEEE Trans. Signal Process. 53(1) 274-282, 2019.
- [21] Tariq Jamil, 2008. Impact of Shift Operations on  $(-1+j)$ -Base Complex Binary Numbers, Journal of Computers, 3(2) 63-71